

# **ANSWER ALL QUESTIONS.**

# **SECTION A**

 $(10 \times 2 = 20)$ 

- 1. Differentiate  $4x^2 9$  with respect to x.
- 2. Find the angle which the tangent at (2, 4) to the curve  $y = 6 + x x^2$  makes with the x-axis
- 3. Evaluate  $\int_{1}^{2} \left(x^2 \frac{1}{x^2}\right) dx$ .
- 4. Integrate  $\int \frac{dx}{x^2 + a^2}$ .
- 5. Prove that  $\frac{e^2 1}{e^2 + 1} = \frac{\frac{1}{1!} + \frac{1}{3} + \frac{1}{5!} + \dots \infty}{1 + \frac{1}{2!} + \frac{1}{4} + \dots \infty}$
- 6. Prove that  $\log \frac{n+1}{n} = 2 \left[ \frac{1}{2n+1} + \frac{1}{3(2n+1)^3} + \frac{1}{5(2n+1)^5} + \cdots \right].$
- 7. Prove that  $cosh2x = cosh^2x + sinh^2x$
- 8. Write the expansion of  $tan5\theta$ .
- 9. What is the chance that a leap year selected at random will contain 53 Sundays?
- 10. Two unbiased dice are thrown. Find the probability of getting an even number on the first die.

## SECTION B

 $(5 \times 8 = 40)$ 

- 11. Find the equation of the tangent to the curve  $y = \frac{6x}{x^2-1}$  at the point (2, 4).
- 12. Evaluate  $\sin^{-1} x dx$ .

**ANSWER ANY FOUR QUESTIONS.** 

- 13. Prove that  $\int_0^{\pi/2} \frac{(sinx)^{3/2}}{(sinx)^{3/2} + (cosx)^{3/2}} dx = \frac{\pi}{4}.$
- 14. Show that  $\log \sqrt{12} = 1 + \left(\frac{1}{2} + \frac{1}{3}\right)\frac{1}{4} + \left(\frac{1}{4} + \frac{1}{5}\right)\frac{1}{4^2} + \left(\frac{1}{6} + \frac{1}{7}\right)\frac{1}{4^3} + \cdots$
- 15. Find the sum to infinity of the series  $\frac{3}{4} + \frac{3.5}{4.8} + \frac{3.5.7}{4.8.12} + \cdots \infty$ .

16. Expand  $sin^4 \theta cos^2 \theta$  in a series of multiples of cosines of multiples of  $\theta$ .

17. If tan(x + iy) = u + iv, prove that  $\frac{u}{v} = \frac{sin2x}{sinh2y}$ .

18. State and prove addition theorem of probability.

## **SECTION C**

# ANSWER ANY TWO QUESTIONS.

19. a) Find the angle of intersection of the cardioids  $r = a(1 + \cos\theta)$  and  $r = b(1 - \cos\theta)$ .

b) Evaluate  $I = \int_0^{\pi/2} logsinxdx$ . (10 + 10)

- 20. a) Solve  $\frac{y^2 z}{x} p + xzq = y^2$  using Lagrange's method. b) Solve  $(D^2 + 3D + 2)y = e^{-x} + x^2 + cosx.$  (10 + 10)
- 21. a) Express  $f(x) = \frac{1}{2}(\pi x)$  as a Fourier series with period  $2\pi$ , to be valid in the interval 0 to $2\pi$ .
  - b) Express  $cos\theta$  in terms of  $sin\theta$ . (12 + 8)
- 22. a) Calculate Mean and Standard deviation for the following table giving the age distribution of 542 members.

Age in	20-30	30-40	40-50	50-60	60-70	70-80	80-90
years							
No. of	3	61	132	153	140	51	2
Members							

b) A car hire firm has two cars, which it hires out day by day. The number of demands for a car on each day is distributed as a Poisson distribution with mean 1.5. Calculate the proportion of days on which (i) neither car is used, and (ii) the proportion of days on which some demand is refused. (10+10)

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## $(2 \times 20 = 40)$